INVESTIGATION OF RADIOLOGICAL PROPERTIES OF IMAGING AGENTS USED IN NUCLEAR MEDICINE WITH DIFFERENT METHODS AND GATE/GEANT4 SIMULATION PROGRAM

by

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Scientific paper https://doi.org/10.2298/NTRP2302116S

This study aims to determine the radiological properties of various radiopharmaceuticals used in nuclear medicine. In the study, mass attenuation coefficient values in different energy ranges were obtained for six different radiopharmaceuticals dimercaptosuccinic acid, diethylenetriamine pentaacetate, mercaptoacetyltriglycine, hexamethylpropyleneamine oxime, methoxyisobutylisonitrile, methylene diphosphate by using GATE simulation program, XCOM and WinXCom programs. Using these values, effective atomic number and electron density values were calculated with the help of the direct method, interpolation method, Auto-Z_{eff} software, Phy-X/ZeXTra, XMuDat program, and Mayneourd's formula. In addition, the effective atomic number and electron density values obtained were compared for each radiopharmaceutical, both among themselves and between the methods. When radiopharmaceuticals were compared among themselves in low and high-energy regions, the highest effective atomic number values were obtained in dimercaptosuccinic acid, methylene diphosphate, and mercaptoacetyltriglycine. The mass attenuation coefficient values calculated using the GATE code indicate that it is a suitable method for determining the mass attenuation coefficient for imaging agents with no experimental values. This study indicates that the simulation geometry method is suitable to be used as an alternative method for the experiments. In addition, the values obtained for these molecules used as radiopharmaceuticals were examined for the first time.

Key words: radiopharmaceuticals, nuclear medicine, effective atomic number, Monte Carlo

INTRODUCTION

The increase in the use of radiation for diagnosis and treatment in fields such as radiology, nuclear medicine, and radiation oncology in recent years has increased the importance of many factors that play an important role in the interaction of radiation with matter. Knowing the physical quantities such as linear attenuation coefficient (μ), mass attenuation coefficient (μ/ρ_m , effective atomic number (Z_{eff}), effective electron density ($N_{\rm eff}$), mass energy absorption coefficient ($\mu_{\rm en}/\rho$ and total atomic cross section (σ_{ta}) and understanding the behavior of gamma and X-ray interactions are essential in medical imaging, radiation dosimetry, and health physics [1, 2]. The (μ/ρ_m) is the basic quantity used to derive parameters such as energy storage, shielding effect, Z_{eff} , and N_{eff} [2-10]. As with pure elements, in photon interactions of composite materials, atomic numbers in the entire energy range cannot be defined by a single number [11]. This number, which is used to characterize composite materials, is called $Z_{\rm eff}$ and has information about the material. The Z_{eff} depends on the incoming energy and the atomic number of the constitutive elements [12, 13]. At a given photon energy, the interaction cross-section is proportional to Zn. The *n* is expected to be between 4 and 5 for the photoelectric effect, 1 for Compton, and 2 for pair formation [14].

The energy range from 5 keV to about 1500 keV is widely utilized in medicine and biological applications [15]. In nuclear medicine departments, radionuclides are used for diagnosis and treatment in similar energy ranges. All of the radionuclides used in nuclear medicine are synthetic and there are many different production methods. Radioactive drugs containing radionuclides in their composition are defined as radiopharmaceuticals that can be used for diagnosis and treatment in nuclear medicine applications [16]. Radiopharmaceuticals consist of two structures. The first structure is the part that emits radiation, called the radionuclide, and the second structure is the part to which the radionuclide, called pharmaceutical, is attached. Radiopharmaceuticals collect in certain tissues or organs, depending on the properties of the drug. Thanks to the radiation emitted by the radionuclide to which it is attached, the structure and

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function of the organs to be imaged can be examined or some tumors and inflammatory diseases can be treated [17]. More than 40 million nuclear medicine procedures are performed each year, and the demand for radionuclides is increasing at an annual rate of 5 % [18]. When radiopharmaceuticals are given for diagnosis or treatment in the nuclear medicine department, the patient is directly exposed to radiation. Therefore, examining the interaction of these pharmaceuticals with radiation gains importance. In the literature, there are many experimental and theoretical studies on effective atomic number, photon attenuation coefficients, electron density, molar attenuation coefficients, total and electronic cross-sections of some organic and inorganic substances, alloys, amino acids, polymers, glasses, various biological compounds [19-23]. However, theoretical studies on $Z_{\rm eff}$, $N_{\rm eff}$, and $(\mu/\rho_m$ for radiopharmaceuticals in nuclear medicine in which diagnostic and therapeutic radiation are used are limited in the literature. Nuclear medicine applications increasing every year, and the demand for the radionuclides used and the limited studies on this subject have prompted us to do this study.

This study aims to determine the radiological properties of various radiopharmaceuticals used in nuclear medicine. In the study, $(\mu/\rho_m \text{ values in different}$ energy ranges were obtained for six different radiopharmaceuticals: dimercaptosuccinicacid (DMSA), diethylenetriamine pentaacetate (DTPA), mercaptoacetyltriglycine (MAG3), hexamethylpropylene-amineoxime (HMPAO), methoxyisobutylisonitrile (MIBI), methylenediphosphate (MDP) by using GATE simulation program, XCOM and WinXCom programs [24, 25]. Using these values, Z_{eff} and N_{eff} values were calculated with the help of the direct

method, interpolation method, Auto- Z_{eff} software [26], Phy-X/ZeXTra, Mayneourd's formula [27], and single-valued XMuDat program [28]. In addition, the $Z_{\rm eff}$ and $N_{\rm eff}$ values obtained were compared for each radiopharmaceutical, both among themselves and between the methods. This information is important clinically and dosimetrically. It is also believed that the results acquired may be useful in various applications (health physics, shielding, water equivalent material, nuclear medicine, radiology, etc.) where radiation is used. The mass attenuation coefficient is important in dosimetry to calculate the attenuation cross-section calculations. In addition, the values obtained for these molecules used as radiopharmaceuticals were examined for the first time. It is also thought to be important for this study.

MATERIAL AND METHODS

Selection of radiopharmaceuticals

In these methods, radiation is emitted from the patient's body thanks to the radiopharmaceuticals applied to the patient, and this emitted radiation is converted into numerical data by the devices used, processed, and an image is obtained. Thanks to these images obtained, functional abnormalities of organs and early imaging of tumors are detected and also useful for treatment planning. Considering all these, radiopharmaceuticals such as DMSA, DTPA, MAG3, HMPAO, MIBI, and MDP, which are frequently used in nuclear medicine, were included in this study. Table 1 shows the list of radiopharmaceuticals with their

Radiopharmaceutical	Chemical formula	Molar mass [gmol ⁻¹]	Mean atomic number
DMSA	C ₄ H ₆ O ₄ S ₂	182.22	6.30
DTPA	C ₁₄ H ₂₃ N ₃ O ₁₀	393.35	4.16
MAG3	C ₈ H ₁₃ N ₃ O ₅ S	263.27	4.63
HMPAO	$C_{13}H_{28}N_4O_2$	272.39	3.19
MIBI	C ₆ H ₁₁ NO	113.16	3.26
MDP	CH ₆ O ₈ P ₂	208.00	6.43

 Table 1. List of radiopharmaceuticals with their chemical formulas

Radionuclide	Physical half-life	Decay mode	Principal E [MeV]	Method of production
¹¹ C	20.4 min	eta^+	0.511	Cyclotron
¹⁸ F	109.8 min	eta^+	0.511	Cyclotron
⁶⁸ Ga	68 min	β^+ , EC	0.511	Generator
⁶⁷ Ga	3.3 d	EC	0.093, 0.185, 0.3	Cyclotron
^{99m} Tc	6.03 h	IT	0.14	Generator
¹¹¹ In	2.8 d	EC	0.173, 0.247	Cyclotron
¹³¹ I	8.02 d	β^-	0.3645	Fission product
²⁰¹ T1	73 h	EC	0.07, 0.167	Cyclotron
¹⁷⁷ Lu	6.65 d	β^-	0.208	Reactor
¹²³ I	13.2 h	EC	0.159	Cyclotron
¹²⁴ I	4.2 d	β^+ , EC	0.511	Cyclotron

EC: electron capture; IT: isomeric transition; β : beta decay

chemical formulas. Some commonly used radionuclides in nuclear medicine are given in tab. 2.

Calculation of $Z_{\rm eff}$ by direct method

The following formula can be used to calculate the $Z_{\rm eff}$ of materials [31]

$$Z_{\text{eff}} = \frac{\frac{f_i A_i}{i} \frac{\mu}{\rho_i}}{\frac{f_i A_j}{Z_j} \frac{\mu}{\rho_j}}$$
(1)

where f_i , μ , ρ , $(\mu/\rho)_i$, A_i , and Z_j are the molar fraction, linear attenuation coefficient, density, mass attenuation coefficient, atomic weight, and atomic number, respectively. With the help of the XCOM program, the total (μ/ρ) of the elements in the materials were found.

Calculation of the attenuation cross-section

The following formula can be used to calculate the attenuation cross-section σ_a values of the compounds

$$\sigma_a = \frac{\frac{\mu}{\rho_m}}{N_i \frac{W_i}{A_i}}$$
(2)

where (μ/ρ_m) is the mass attenuation coefficient of the material, $N[g^{-1}]$ – the Avogadro's constant in atom, W_i – the weight fraction of the *i*-th element in a molecule of tissue substitute material, and A_i – the atomic weight of the *i*-th element in a molecule. The W_i and A_i are dimensionless. To calculate the Z_{eff} , the calculated attenuation cross-section values were interpolated for the elements produced at the desired energies in WinXCom using the logarithmic formula

$$Z_{\text{eff}} = \frac{Z_1(\log \sigma_2 - \log \sigma_a) - Z_2(\log \sigma_a - \log \sigma_1)}{\log \sigma_2 - \log \sigma_a} (3)$$

where, σ_1 and σ_2 are the elemental cross-sections (barn per atom) in between which the atomic cross-section σ_a of the materials and Z_1 and Z_2 are atomic numbers of the elements corresponding to the cross-sections σ_1 and σ_2 , respectively.

Calculation of Z_{eff} by XMuDat

The XMuDat computer program can produce a single value Z_{eff} for compounds [28]. The following formula can be used to calculate the Z_{eff} of materials for the XMuDat

$$Z_{\text{eff},\text{XMuDat}} = \frac{(\alpha_i Z_i^{m-1})}{m-1}$$
(4)

where α_i is the fractional number of the electrons of the *i*-th element and *m* – the a constant between 3 and 5. It is preferred that *m* is set to 3.6 for materials with $Z_{\text{eff}} < 6$ and 4.1 for materials with $Z_{\text{eff}} > 6$ [32].

Calculation of Z_{eff} by Auto- Z_{eff}

The Auto- Z_{eff} program is used for rapid calculation of the energy-dependent effective atomic number, average atomic numbers, and spectral weighted average atomic numbers. The calculation of the coefficients for the materials is related to the linear addictiveness of the fractional components and is compared with the previously calculated matrix at the separate energies. Therefore, effective atomic numbers are obtained through interpolation of adjacent cross-section data [26, 33].

Calculation of Z_{eff} by Phy-X/ZeXTRa

The Phy-X/ZeXTRa is a new web program for calculating Z_{eff} values for photons, electrons, protons, alpha particles, and carbon ions [27]. For photons, this program uses the cross-section libraries from the WinXCom [25].

Calculation of electron density (N_{eff})

The following formula can be used to calculate the electron density [31]

$$N_{\text{eff}} = N_A \frac{Z_{\text{eff}} n}{n_i A_i} = N_A \frac{Z_{\text{eff}}}{A} (\text{elektron } g^{-1})$$
(5)

where $\langle A \rangle$ is the average atomic mass of materials, N_A – the Avogadro's number, and Z_{eff} is the effective atomic number.

Calculation of $Z_{\rm eff}$ Mayneourd's formula

The effective atomic number Z_{eff} was first calculated using the Mayneord formula [34-36]

$$Z_{\text{eff}} = \frac{\alpha_i Z_i^{2.94}}{\alpha_i Z_i^{2.94}}$$
(6)

where α_i is the relative electron fraction of the *i*-th element and Z_i - the atomic number of each element [37].

The GATE/Geant4 simulation program

The $(\mu/\rho_m$ values were obtained using the GATE v8.1 simulation program at 10 keV, 50 keV, 100 keV, 140 keV, 364 keV, 511 keV, 1022 keV,

1250 keV, and 1500 keV energies and 10 m × 10 m field size with a source-surface distance of 100 cm. The main volume with 10 m × 10 m × 10 m size was filled with air. Then, the Fluence Actor was located in the defined volume at a 100 cm distance from the source to determine how many particles passed through it. The fraction weight of imaging agents and selected human organs and their concentration were classified inside the *Gatematerial list*. The number of histories for all simulations was 2×10^8 [10, 23].

RESULT AND DISCUSSION

The $(\mu/\rho_m$ values of DMSA, DTPA, MAG3, HMPAO, MIBI, and MDP for photon energies ranging from 1 keV to 100 MeV, fig. 1. Radiopharmaceuticals consist of elements with atomic numbers (Z) ranging from 1 to 16 (H:1, C:6, N:7, O:8, P:15, S:16). In fig. 1, it was observed that the (μ/ρ_m) values of all radiopharmaceuticals were maximum at 1 keV energy, and the $(\mu/\rho_m$ values decreased rapidly with increasing photon energy over the range of 0.01 to 0.1 MeV. Up to 10 MeV (μ/ρ_m) values continue to decrease. However, since radiopharmaceuticals such as MDP, DMSA, and MAG3 contain elements with high atomic numbers such as 16S and 15P, their decay rate is slower than others. These elements have a sudden jump in (μ/ρ_m) values, around 3 keV, due to K-edge absorption. The sharp decrease up to 0.1 MeV can be explained by the fact that photoelectric absorption is more dominant at lower energies, especially for elements with high atomic numbers. In the energy range where photoelectric absorption is dominant, the photon interaction cross-section depends on Z4-5 and E³ [38-40].

Figure 1 shows the variation of radiofarmaceuticals with $(\mu \rho)_m$ for various photon energy. The Z_{eff} calculated by various methods in the 10 keV to 1 GeV photon energy region are shown in fig. 2. Z_{eff} below 10 keV energy were not compared due to uncertainty (25 %) in Auto- Z_{eff} [26]. It has been found that Auto- Z_{eff} , Phy-X/ZeXTRa, direct and interpolation methods are in harmony with the Z_{eff} calculation in the 50 keV and 20 MeV energy regions where the component interaction process is dominant. While the effective atomic number was found to be constant in the medium energy photon region, significant differences were found in the low (<30 keV) and high (>20 MeV) photon regions. The (μ/ρ_m) obtained with XCOM and GATE are given in tab. 3 (μ/ρ_m) for imaging agents were obtained using GATE and different methods and are presented in tab. 4.

The (μ/ρ_m) of selected human organs were found using the GATE simulation program to validate the measurement geometry and functioning before the results were obtained. These results were compared with values obtained from XCOM. It was found that the (μ/ρ_m) values for the selected human organs were very close to theoretical XCOM data results. The (μ/ρ_m) values of imaging agents were obtained using GATE at various photon energies and compared with different methods. Thus, it has been observed that the GATE simulation program provides photon interaction parameters for imaging agents. The (μ/ρ_m) values obtained using the GATE simulation program were in good agreement with the results obtained by different methods, tab. 3.

The Zeff values calculated by Phy-X/ZeXTra and the direct method were higher in the photoelectric absorption and pair formation regions when compared to the Z_{eff} values calculated by the Auto- Z_{eff} and interpolation method. In the energy region where pair formation is dominant, the difference between $Z_{\rm eff}$ values is less than in the photoelectric absorption region. Büyükyildiz stated in his study [41] that the differences between the $Z_{\rm eff}$ obtained by direct and interpolation methods in the energy region where the photoelectric effect is dominant are large and not uniform. It is thought to be due to the non-uniform variation of (μ/ρ_m) in this energy region. Similar results were obtained in our study. In addition, since the Z_{eff} has more than one value for the direct and interpolation method at the K absorption edge, which corresponds to the high Z element in radiopharmaceuticals, the two methods do not give compatible results with each other. In



Figure 1. Variation of $(\mu/\rho_m \text{ with } photon \text{ energy for various } radiopharmaceuticals$



Figure 2. The $Z_{\rm eff}$ of radiopharmaceuticals calculated by different methods

direct and interpolation methods, different weights are given to individual atomic numbers when calculating the weighted average [42]. It can be said that these differences are because the absorption processes depend on the atomic number and energy. The $Z_{\rm eff}$ calculated using the XMuDat program of DMSA, DTPA, MAG3, HMPAO, MIBI, and MDP were found as 12.12, 6.90, 9.50, 6.22, 6.21, 11.13, respectively. The single-valued $Z_{\rm eff}$ and $N_{\rm eff}$ have been calculated for radiopharmaceuticals using the XMuDat program. It was seen that significant differences occur between the single-valued $Z_{\rm eff}$ and the $Z_{\rm eff}$ obtained for different energies, fig. 2. It is recommended that the XMuDat program can be used with safety at low photon energies up to 0.01 MeV where photoelectric absorption predominates for calculation of $Z_{\rm eff}$ and $N_{\rm eff}$ since it gives values close to the ones obtained with the energy-dependent Mayneourd's formula. Similar results were obtained in Kurudirek 's study [34]. Since the radiation energy used in nuclear medicine is for diagnostic purposes, their energies are quite low. Therefore, lower energies are preferred in tabs. 5 and 6.

As in other literature studies [3, 12, 27, 39], it was found that the $Z_{\rm eff}$ values calculated by all four methods in the Compton scattering region and the calculation methods used were compatible, but there was a difference between the $Z_{\rm eff}$ values in the photoelectric and pair formation regions.

CONCLUSIONS

In the energy region between 1 keV and 100 GeV, Z_{eff} and N_{eff} values for DMSA, DTPA, MAG3, HMPAO, MIBI, and MDP used in nuclear medicine were calculated using four different methods. While the Z_{eff} values obtained depend on the chemical compound of the material at low and high energies, it is observed that this dependence weakens in the middle energy region. The values obtained as a result of the Neff calculation are closely related to Z_{eff} and N_{eff} 's tendency towards energy was found to be similar to Z_{eff} 's for all samples. While these four methods give good results in the Compton scattering region for the new

	Energy [keV]												
Materials	14	40	30	364		11	1022						
	XCOM	GATE	XCOM	GATE	XCOM	GATE	XCOM	GATE					
aWater	0.1531	0.1528	0.1102	0.1095	0.0956	0.0953	0.0692	0.0679					
^a Soft tissue	0.1524	0.1515	0.1093	0.1094	0.0944	0.0941	0.0691	0.0677					
^a Muscle	0.1521	0.1502	0.1094	0.1087	0.0953	0.0943	0.0697	0.0685					
^a Bone	0.1526	0.1534	0.1103	0.1089	0.0917	0.0920	0.0664	0.0671					
^a Brain	0.1534	0.1517	0.1095	0.1087	0.0952	0.0947	0.0696	0.0673					
^a Breast	0.1527	0.1524	0.1097	0.1081	0.0954	0.0946	0.0695	0.0692					
^a Testis	0.1535	0.1512	0.1099	0.1083	0.0954	0.0962	0.0695	0.0689					
^a Eye	0.1516	0.1501	0.1083	0.1087	0.0946	0.0942	0.0689	0.0681					
^a Adipose	0.1517	0.1516	0.1084	0.1097	0.0946	0.0944	0.0689	0.0677					
^a Lung	0.1523	0.1527	0.1091	0.1076	0.0951	0.0952	0.0693	0.0682					
^a Blood	0.1524	0.1505	0.1092	0.1085	0.0951	0.0951	0.0693	0.0682					
DMSA	0.1491	0.1485	0.1034	0.1026	0.0891	0.0887	0.0652	0.0638					
DTPA	0.1464	0.1417	0.1055	0.1039	0.0914	0.0904	0.0661	0.0645					
MAG3	0.1473	0.1468	0.1047	0.1037	0.0905	0.0912	0.0665	0.0647					
НМРАО	0.1515	0.1489	0.1096	0.1068	0.0952	0.0945	0.0694	0.0678					
MIBI	0.1502	0.1517	0.1087	0.1068	0.0943	0.0927	0.0697	0.0681					
MDP	0.1451	0.1441	0.1013	0.1021	0.0881	0.0878	0.0643	0.0642					

Table 3. Comparison of $(\mu/\rho_m [cm^2g^{-1}])$ in energies commonly used in nuclear medicine with XCOM and GATE results

^aICRU Report 44, Tissue Substitutes in Radiation Dosimetry and Measurement, Bethesda (MD), USA, 2023

Table 4	. (Comparison	of the	(μ/ρ	m	[cm ²	g_	¹]obtained f	for some	energies	with	the	different	methods
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Matariala	Mathad	Energy [MeV]								
Materials	Method	0.01	0.05	0.10	1.25	1.50				
DMSA	XCOM	20.371	0.341	0.175	0.058	0.053				
	Phy-X/ZeXTRa	20.404	0.341	0.175	0.065	0.054				
	XMuDat	20.373	0.337	0.168	0.066	0.054				
	GATE	20.072	0.338	0.165	0.058	0.056				
	XCOM	3.873	0.207	0.161	0.060	0.054				
	Phy-X/ZeXTRa	3.872	0.207	0.161	0.063	0.054				
DIPA	XMuDat	3.851	0.204	0.168	0.059	0.055				
	GATE	3.867	0.206	0,163	0.061	0.057				
	XCOM	9.418	0.252	0.166	0.059	0.054				
MAG2	Phy X/ZeXTRa	9.418	0.252	0.167	0.059	0.054				
MAGS	XMuDat	9.405	0.246	0.167	0.058	0.053				
	GATE	9.407	0.249	0.164	0.055	0.055				
	XCOM	2.897	0.207	0.166	0.062	0.057				
	PhyX/ZeXTRa	2.897	0.208	0.165	0.063	0.057				
IMITAU	XMuDat	2.883	0.216	0.158	0.064	0.054				
	GATE	2.889	0.205	0.155	0.063	0.052				
	XCOM	2.871	0.206	0.166	0.062	0.056				
MIDI	Phy-X/ZeXTRa	2.870	0.206	0.165	0.062	0.056				
IVIIDI	XMuDat	2.856	0.215	0.158	0.061	0.055				
	GATE	2.868	0.220	0.163	0.063	0.056				
	XCOM	15.831	0.298	0.168	0.058	0.052				
MDD	Phy-X/ZeXTRa	15.831	0.297	0.168	0.057	0.052				
MDP	XMuDat	5.828	0.307	0.161	0.058	0.053				
	GATE	15.819	0.299	0.170	0.059	0.055				

materials to be $Z_{\rm eff}$ calculated, they give different $Z_{\rm eff}$ values in the low and high-energy regions. Therefore, $Z_{\rm eff}$ values need more experimental accuracy, especially in high and low-energy regions. When radiopharmaceuticals were compared among themselves in low and high-energy regions, the highest $Z_{\rm eff}$ values were obtained in DMSA, MDP, and MAG3, re-

spectively. The lowest Z_{eff} value was obtained in DTPA, MIBI, and HMPAO. The Monte Carlo simulated (μ/ρ_m for the imaging agents in some photon energies were found to be very close to the theoretical XCOM values and GATE simulation program. This study indicates that the simulation geometry method is suitable to be used as an alternative method for the ex-

De l'este service le	Madaad	Energy [MeV]								
Radiopharmaceuticais	Method	0.01	0.05	0.1	1.25	XMuDat	Mayneourd			
	Direct	13.75	8.21	6.33	5.87					
DMSA	Interpolation	9.90	8.62	6.57	5.89	12.12	11.71			
	Auto-Z _{eff}	9.88	8.60	6.55	5.88					
	Phy-X/ZeXTRa	13.75	8.20	6.33	5.88					
	Direct	6.99	4.42	4.21	4.16					
DTDA	Interpolation	6.10	4.59	4.26	4.17	6.90	6.82			
DIFA	Auto-Z _{eff}	6.07	4.58	4.24	4.16					
	Phy-X/ZeXTRa	7.00	4.42	4.20	4.16					
	Direct	10.96	5.62	4.80	4.63					
MAC2	Interpolation	7.70	5.94	4.86	4.61	9.50	9.04			
MAGS	Auto-Z _{eff}	7.69	5.93	4.85	4.60					
	Phy-X/ZeXTRa	10.95	5.59	4.77	4.61					
	Direct	6.19	3.37	3.23	3.19					
	Interpolation	5.24	3.49	3.26	3.18	6.22	6.13			
IMITAO	Auto-Z _{eff}	5.21	3.47	3.24	3.19					
	Phy-X/ZeXTRa	6.18	3.37	3.23	3.19					
	Direct	6.20	3.45	3.29	3.26					
MIDI	Interpolation	5.26	3.56	3.34	3.27	6.21	6.12			
MIBI	Auto-Z _{eff}	5.24	3.54	3.31	3.26					
	Phy-X/ZeXTRa	6.19	3.44	3.30	3.26					
	Direct	12.24	7.91	6.56	6.24					
MDD	Interpolation	9.46	8.32	6.75	6.25	11.13	10.81			
WIDP	Auto-Z _{eff}	9.44	8.30	6.74	6.23					
	Phy-X/ZeXTRa	12.24	7.90	6.56	6.23					

Table 5. The $Z_{\rm eff}$ of radiopharmaceuticals calculated by the Auto- $Z_{\rm eff}$, Phy-X/ZeXTRa, direct, interpolation, XMuDat, and Mayneourd's formula

Table 6. The $N_{\rm eff}$ (10^{23} g⁻¹) of radiopharmaceuticals calculated by the Auto- $Z_{\rm eff}$, Phy-X/ZeXTRa, direct, interpolation, XMuDat, and Mayneourd's formula

	Mathal	Energy [MeV]									
Radiopharmaceuticais	Method	0.01	0.05	0.1	1.25	XMuDat	Mayneourd				
	Direct	7.27	4.33	3.35	3.11						
DMCA	Interpolation	5.23	4.56	3.47	3.12	3.11	3.51				
DMSA	Auto-Z _{eff}	7.26	4.54	3.46	3.11						
	Phy-X/ZeXTRa	5.24	4.34	3.34	3.11						
	Direct	5.35	3.38	3.22	3.18						
DTDA	Interpolation	4.66	3.52	3.25	3.19	3.18	3.11				
DIPA	Auto-Z _{eff}	4.65	3.51	3.24	3.19						
	Phy-X/ZeXTRa	5.34	3.39	3.24	3.18						
	Direct	7.52	3.86	3.30	3.18						
MAC2	Interpolation	5.28	4.07	3.33	3.16	3.16	3.52				
MAG3	Auto-Z _{eff}	7.51	3.83	3.32	3.15						
	Phy-X/ZeXTRa	5.28	4.05	3.28	3.16						
	Direct	6.43	3.51	3.35	3.32						
	Interpolation	5.42	3.60	3.37	3.30	3.32	3.14				
HMPAO	Auto- $Z_{\rm eff}$	6.42	3.59	3.37	3.31						
	Phy-X/ZeXTRa	5.43	3.50	3.35	3.32						
	Direct	6.26	3.48	3.33	3.30						
MIDI	Interpolation	5.30	3.58	3.35	3.30	3.30	3.13				
MIBI	Auto-Z _{eff}	5.29	3.58	3.35	3.31						
	Phy-X/ZeXTRa	6.26	3.49	3.36	3.30						
	Direct	6.02	3.89	3.22	3.06						
MDD	Interpolation	4.65	4.08	3.32	3.07	3.07	3.29				
MDP	Auto-Z _{eff}	6.64	4.08	3.31	3.06						
	Phy-X/ZeXTRa	6.03	3.89	3.23	3.07						

periments. It is thought that it would be beneficial to use $\mu/\rho Z_{\rm eff}$, and $N_{\rm eff}$ values obtained by different methods in various applications such as health physics, engineering, and medical dosimetry.

AUTHORS' CONTRIBUTIONS

T. Sahmaran: Conceptualization, methodology, formal analysis, calculations, and analyses – writing the original draft. T. Tugrul: Conceptualization, methodology, original draft, writing – review and editing.

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Received on March 17, 2023 Accepted on September 26, 2023

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ИСТРАЖИВАЊЕ РАЗЛИЧИТИМ МЕТОДАМА И GATE/GEANT4 ПРОГРАМОМ СИМУЛАЦИЈЕ РАДИОЛОШКИХ СВОЈСТВА АГЕНАСА СЛИКЕ КОЈИ СЕ КОРИСТЕ У НУКЛЕАРНОЈ МЕДИЦИНИ

Циљ рада је да се утврде радиолошка својства различитих радиофармацеутика који се користе у нуклеарној медицини. Коришћењем GATE програма за симулацију, XCOM и WinXCom програма, добијене су вредности масених коефицијената слабљења у различитим енергетским опсезима за шест различитих радиофармацеутика: димеркаптосукцинске киселине, диетилентриамин пента-ацетата, меркапто-ацетил триглицина, хексаметилпропиленамин оксима, метокси-изобутил-изонитрила и метилен дифосфата. Користећи ове вредности, израчунати су ефективни атомски број и вредност густине електрона уз помоћ директне методе, методе интерполације, Auto-Zeff софтвера, Phy-X/ZeXTra и XMuDat програма и Мајнардове формуле. Поред тога, добијене вредности ефективног атомског броја и густине електрона упоређене су за сваки радиофармацеутик, како између њих, тако и између метода. Када су радиофармацеутици међусобно упоређивани у регионима ниске и високе енергије, највеће ефективне вредности атомског броја добијене су у димеркаптосукцинској киселини, метилен дифосфату и меркапто-ацетил триглицину. Вредности масених коефицијената слабљења израчунате коришћењем GATE програма указују на то да је то примерена метода за одређивање масених коефицијената слабљења агенаса за снимање без експерименталних вредности. Рад показује да је метода геометријске симулације погодна за примену као алтернативна метода експериментима. Поред тога, по први пут испитане су вредности добијене за ове молекуле који се користе као радиофармацеутици.

Кључне речи: фармацеушик, нуклеарна медицина, ефекшивни ашомски број, Монше Карло мешода